The effect of lesion size and tissue remodeling on ST deviation in partial-thickness ischemia

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BACKGROUND Myocardial ischemia causes ST segment elevation or depression in electrocardiograms and epicardial leads. ST depression in epicardium overlying the ischemic zone indicates that the ischemia is nontransmural. However, nontransmural ischemia does not always cause ST depression. Especially in animal models, ST depression is hard to reproduce.

OBJECTIVE The purpose of this study was to determine the circumstances in which ST depression could be expected.

METHODS We studied ischemia in a large-scale computer model of the human heart. A realistic representation of the ischemia-induced changes in resting membrane potential was used, which was based on diffusion of extracellular potassium. Ischemia diameter, transmural extent, and tissue conductivity were varied.

RESULTS Our simulations confirm earlier work showing that partial-thickness ischemia, like full-thickness ischemia, typically causes ST elevation in an anisotropic model of the ventricles. However, we identified three situations in which ST depression can occur in overlying leads. The first is a reduced anisotropy ratio of the intracellular conductivity, which may result from hypertrophy and gap-junctional remodeling, circumstances that are likely to accompany ischemia. Second, an increase of the extracellular anisotropy has the same effect. Third, ST depression was found, independent of the anisotropy ratios, in very large and thin ischemic regions, resembling those that may occur in left-main or multivessel disease.

CONCLUSION Both tissue remodeling and geometric factors can explain ST depression in overlying epicardial leads. We note at the same time that ST elevation is found in most circumstances, while depression occurs as a reciprocal effect, even in partial-thickness ischemia.

KEYWORDS Ischemia; ST deviation; NSTEMI; Gap junctions; Tissue remodeling; Computer model; Extracellular potassium

Introduction

Myocardial ischemia can cause elevation and depression of the ST segment in electrocardiograms (ECGs) and epicardial electrograms. Elevation is a sign of myocardial infarction due to complete occlusion of a coronary artery. Depression, especially in leads proximal to the occluded artery,2–6 is related to incomplete occlusion and is thought to be mediated by subendocardial ischemia.7,8

In ischemic tissue the resting membrane potential (V_m) is depolarized with respect to normal tissue. This leads to a depression of the TQ segment in the local extracellular electrogram.9–11 With the customary AC-coupled amplifiers, the TQ segment must be defined as isoelectric, so the change is observed as an elevation of the ST segment. In addition, true ST elevation can develop in advancing ischemia because of a reduction of action potential amplitude and duration.12 For convenience, we describe both TQ and ST changes as ST segment deviations.

Elevation of the ST segment is observed in epicardial leads overlying a transmural ischemia.12 Depression in overlying leads can only occur in partial-thickness ischemia.13 In epicardial leads, ST depression has been observed when subendocardial ischemia or injury was produced in the in situ dog heart.11,13 These studies suggested that the ST depression area on the epicardium coincided with the ST elevation area on the endocardium. However, in other studies the deepest ST depression was located over a lateral border of the ischemia,14,15 and the negative zone on the epicardium did not move during a transition from partial-thickness to full-thickness ischemia.15 Thus, partial-thickness ischemia alone cannot explain ST depression.

Recent computer simulations have predicted ST elevation in epicardial leads overlying a partial-thickness ischemia,16,17 while ST depression was found adjacent to the...
ischemic area. These studies were based on realistic conductivity values for healthy myocardium. However, ischemic myocardium is likely to have been ischemic before or to show other symptoms of heart failure. Its conductivity may be modified because of hypertrophy and redistribution of gap junctions.18–24

The distinction between ST elevation and ST depression is central to the analysis of ECG changes in patients with acute coronary syndromes. Therefore, a good understanding of the mechanisms underlying ST elevation/depression is required. Understanding of the epicardial ST deviations that are observed in experimental models provides an important part of the overall picture. In this study, we use a computer model of the human heart with a realistic representation of the ischemic zone to identify the factors that can account for ST depression in leads overlying a subendocardial ischemic area.

Methods

Extracellular potentials were simulated with a computer model of the human heart that has been described elsewhere.25 Briefly, the heart was discretized in three dimensions at 0.25-mm resolution. Extracellular potentials were computed at 22 million nodes connected with an anisotropic bidomain tissue model26,27 incorporating a transmural fiber rotation. Since we were only interested in the amount of ST deviation, we did not simulate propagation. Instead, we used a fixed distribution of resting $V_m$. The model then computed the corresponding extracellular potentials.

The $V_m$ pattern was based on a computed distribution of extracellular K$^+$ concentration ([K$^+]_o). To obtain this distribution, we assumed that in ischemic myocardium K$^+$ is extruded from the cells at a rate of 13 $\mu$M/s,28,29 while normal, perfused myocardium maintains its [K$^+]_o$ near 5 mM. A discrete boundary between normal and ischemic regions was used to represent the very narrow metabolic border.30–32 In addition, we reckoned that K$^+$ diffuses through the myocardium even in ischemic regions.28 The distribution of [K$^+]_o$ can then be described by a diffusion equation33 with source term $S$:

$$ \frac{\partial [K^+]_o}{\partial t} = D \nabla^2 [K^+]_o + S, $$

where $D$ is the apparent diffusion constant of the tissue for K$^+$ ions

(1) $S = 13 \mu$M/s for ischemic myocardium and

(2) $S = g \cdot (5 \text{ mM} - [K^+]_o)$ elsewhere,

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**Figure 1**

**A:** Transverse and longitudinal sections of the model anatomy, with normal myocardium shown as green, blood as blue, and connective tissue as gray. The horizontal line in each slice indicates where the other slice was taken. A color scale from black through red to white indicates resting $V_m$ in the ischemic region, ranging from $-91$ to $-65$ mV. The normal myocardium, although shown in a different color, has the same resting potential of $-91$ mV as the very border of the ischemic zone. The ischemic region in this example had diameter $d = 30$ mm and extent $e = 50\%$. The $V_m$ profile along the line shown in the upper two panels is depicted in the lower panel. The profile is approximately parabolic with a slightly rounded foot. **B:** ST deviations in the extracellular domain. Potential differences are shown as pseudocolors; the scale is in millivolts. Upper panel: normal $R_l = 10$. Lower panel: isotropic intracellular domain. In the normal anisotropic case, ST elevation is measured on the epicardium. In the isotropic case, ST depression is obtained. Because of the anisotropy of the extracellular domain and the conductivity of the cavity blood, the epicardium is then more negative than the endocardium adjacent to the ischemia. The geometry of the ischemic region is shown in panel A.
where \( g \) is a constant that describes the capacity of the perfusion to remove \( K^+ \) from the extracellular space. Expression (3) was applied in the normal myocardium, connective tissue, and intracavitary blood. Since both \( D \) and \( g \) are unknown, we chose \( g = 5 \) s\(^{-1}\) and scaled \( D \) such that \([K^+]_o\) in the center of the ischemic zone was 14 mM. No-flow boundary conditions were used at the tissue-air and blood-air interfaces (Figure 1A). By integrating equation (1) through time until a stable state was reached, we obtained a distribution of \([K^+]_o\) throughout the heart. Using a mathematical model of the human ventricular cell membrane,\(^{34}\) we translated the \([K^+]_o\) value into a \( V_m \) for each node. The influence of \( V_m \) on the \( K^+ \) extrusion rate was ignored.

By considering only changes in resting \( V_m \), we simulated TQ segment changes. For convenience, we will describe these as apparent ST segment changes. True ST segment changes (due to changes in action potential duration and plateau potential) were ignored. This should not affect our results in a significant way because the effects of true ST segment changes only amplify those of the apparent ST segment changes.

A subendocardial ischemic region was assumed in the lateral wall of the left ventricle. Several different geometries were explored, characterized by a diameter \( d \) (in millimeters) and a transmural extent \( e \) given as a percentage. An example of such a region and the computed offsets in resting \( V_m \) are shown in Figure 1A.

The bidomain model represents the myocardium by two co-located syncytia, called the “intracellular domain” and “extracellular domain,” each characterized by anisotropic conductivities (Table 1). The intracellular domain represents the cells and gap junctions, while the extracellular domain represents the interstitium and small blood vessels.\(^{35}\) The anisotropy ratios of the conductivities of the two domains will be denoted by \( R_i \) and \( R_e \), respectively. To implement gap-junctional remodeling with the bidomain model, we varied \( R_i \) stepwise around its normal value of 10 by modifying the longitudinal conductivity \( \sigma_{IL} \). Intracavitary blood and connective tissue were isotropic and had no intracellular domain.

### Results

Figure 1B shows simulated extracellular potentials in a section of the heart. In a normal anisotropic intracellular domain, injury current flows mainly along the fibers. This creates two current sinks in the extracellular domain adjacent to the ischemic area and a positive area on the epicardial side, as explained previously by Hopenfeld et al.\(^{16}\) On the epicardium directly overlying the center of the ischemic area, the extracellular potential is positive.

In contrast, in a fully isotropic intracellular domain, current flows equally in all directions. This leads to a current sink area in the extracellular domain surrounding the ischemic area. The epicardium overlying the ischemia now shows a negative potential. The anisotropy of the extracellular domain makes the overlying epicardium more negative than the endocardium adjacent to the ischemia. This effect is enhanced by the intracavitary blood.

The results shown above apply to the two extreme cases: normal anisotropic (\( R_i = 10 \)) and isotropic (\( R_i = 1 \)). We also investigated intermediate anisotropy ratios. The ST deviation measured on the epicardium in the center of the ischemic region is shown in Figure 2. The ST deviation is seen to reduce gradually with a reduction in anisotropy ratio and to become negative when \( R_i \leq 3 \). The analysis was repeated with the intracavitary blood removed. In this case, the ST elevations were much larger and reversal occurred only at \( R_i \leq 2.5 \). All further experiments were performed with blood-filled cavity.

The effect of transverse conductivity was also investigated. In Figure 3, the ST deviation is again considered as a function of \( R_i \) for two different values of transverse con-
ductivity. The two curves are nearly coincident, demonstrating that conductivity changes without change in anisotropy ratio have only a limited effect; increased conductivity increases ST depression notably at low $R$. The anisotropy ratio is the main determinant of the sign of ST deviation.

The anisotropy ratio of the extracellular domain, $R_e$, also affects ST deviation, as shown in Figure 4. Increased $R_e$ decreases ST elevation and increases ST depression. In the presence of a doubled $R_e$, a slightly reduced value of $R_i = 7$ would already cause ST depression.

Figure 5 shows the effect of ischemic geometry on the epicardial ST deviation. It demonstrates that larger diameter and smaller transmural extent favor ST depression. Depression is obtained for all tested $R_i$ when $d = 75 \text{ mm}$ and $e \leq 30\%$. This corresponds to a thin ischemic area that covers more than half of the left ventricular endocardium. With a larger diameter, the magnitude of the ST deviation can be larger.

**Discussion**

The classical theory of ST depression overlying an ischemic zone is often illustrated with a cartoon such as the one shown in Figure 6A. Recent experimental and theoretical studies, however, showed elevation in overlying epicardium. The reason for the discrepancy is that the classical theory does not account for anisotropy.

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**Figure 3** Effect of conductivity in the intracellular domain. The ST deviation is shown as a function of $R_i$. Thick line: $\sigma_{\text{it}} = 0.3$; thin line: $\sigma_{\text{it}} = 0.6 \text{ mS/cm}$. The geometry of the ischemic region was $d = 30 \text{ mm}$ and $e = 50\%$. By itself, $\sigma_{\text{it}}$ turns out to have little effect; the anisotropy ratio is the primary determinant of ST deviation.

**Figure 4** Effect of increased $R_e$. The ST deviation is shown as a function of $R_i$. Upper curve: normal $R_e = 2.5$ ($\sigma_{\text{eT}} = 1.2$, $\sigma_{\text{eL}} = 3.0$), as in Figure 2. Lower curve: increased $R_e = 5.0$ due to a reduced transverse component ($\sigma_{\text{eT}} = 0.6$, $\sigma_{\text{eL}} = 3.0$). The geometry of the ischemic region was $d = 30 \text{ mm}$ and $e = 50\%$.

**Figure 5** Effect of diameter and extent of the ischemic region. The ST deviation is shown as a function of $R_i$. In the upper panel, the diameter is fixed at $25 \text{ mm}$, while the transmural extent is varied from $30\%$ to $70\%$. For every extent value, ST depression is found when the intracellular domain is nearly isotropic. The range of anisotropy values for which ST depression is obtained is larger for thinner ischemic regions. In the lower panel, the diameter is $75 \text{ mm}$, and the same values of transmural extent are shown. The relation between anisotropy ratio and ST deviation is similar to the $25\text{-mm}$ case, but the curves are steeper and, more importantly, shifted downward. For this diameter, ST depression can be obtained with normal anisotropy and a transmural extent of $30\%$. 

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Figure 6B explains ST elevation in epicardial leads overlying a subendocardial ischemia. For convenience, it will be described in terms of resistances rather than conductivities. The figure shows a transmural section of the ventricle. This section is shown twice: once for the intracellular and once for the extracellular domain. The shaded area indicates an ischemic zone. Its exact shape and size are unimportant in this treatment. Electric current is confined to a system of wires and resistors. All resistors have the same value; higher directional resistances are depicted with two or three resistors. The repartition of the resistors represent the fact that \( R_i > R_e \). The cellular membrane is represented by potential sources, which have zero potential in the healthy tissue and unit potential in the ischemic area. The potential difference between the two areas then causes an extracellular current to flow from the ischemic to the healthy myocardium, returning through the intracellular domain. The current that passes through the epicardium encounters two resistors in the extracellular and three in the intracellular domain. Therefore, the potential at the epicardium is 3/5.

The current through the healthy endocardium encounters the same resistance in the intracellular as in the extracellular domain; hence the potential is 1/2 in the healthy endocardium. The extracellular potential is thus larger on the epicardium than on the healthy endocardium, which indicates an epicardial ST elevation. Figure 6C shows a similar model of isotropic tissue. In this case, no potential difference between the epicardial and lateral borders of the ischemia results. These predictions agree with the results of our more realistic model when the intracavitary blood is ignored (Figure 2). Both models predict ST depression when \( R_i < R_e \). In a model where \( R_i = R_e = 1 \), epicardial ST depression occurs only due to the intracavitary blood.

**Ischemia and remodeling**

Myocardial ischemia often occurs with preexisting tissue remodeling, especially when it is chronic or recurrent. An important aspect of remodeling is the redistribution of gap junctions.\(^{22}\) Gap junctions provide an electrically conducting pathway between cardiac myocytes. They are preferentially located in the intercalated disks (IDs). Gap junctions are formed by large proteins known as connexins. In human ventricular myocardium, connexin 43 (Cx43) is the most important of these.\(^{37}\) Ischemia reduces the expression of phosphorylated Cx43\(^{38,39}\) and gap-junctional area.\(^{19}\) Reperefusion causes a return of phosphorylated Cx43, which is then more equally distributed along the membrane.\(^{21,23}\) It is not known if the reappearing connexins are part of functional gap junctions. Both the disappearance of Cx43 from the ID and the formation of lateral gap junctions would contribute to reduced \( R_i \). According to our results, this would favor ST depression (Figure 2). The conductivity of gap junctions is also modulated by pH and intracellular \([\text{Ca}^{2+}]\).\(^{21,40}\) These factors too may be modified in ischemic myocardium, but they would only affect ST deviation if they change longitudinal and transverse conductivity differently (Figure 3). Reduction and lateralization of gap junctions have also been related to heart failure\(^{24,41}\) and more specifically to hypertrophy.\(^{19,20,22}\) Uzzaman et al\(^{22}\) observed a 31% decrease in gap junction area in hypertrophic rat myocardium, with a reduction of anisotropy in propagation velocity. Cooklin et al\(^{20}\) provided direct proof of reduced longitudinal conductivity.

**ST deviation in experimental ischemia**

Experimental studies of subendocardial ischemia demonstrated both ST elevation and ST depression on epicardium overlying a subendocardial ischemia. Guyton et al\(^{13}\) found progressive epicardial ST depression during partial occlusion of the left circumflex artery (LCX) in dogs. Similarly, Hellerstein and Katz reported ST depression in epicardial leads overlying a zone of endocardial injury.\(^{11}\) During occlusion of either the LCX or the left anterior descending artery (LAD), Li et al\(^{14}\) found a zone of epicardial ST depression centered not on the ischemic area, but on its lateral border. Kilpatrick et al\(^{15}\) showed that this negative zone is not displaced during a transition from subendocardial to transmural ischemia.
Results of this study
We found that ST depression on epicardium overlying a subendocardial ischemia can occur due to (1) reduced \( R_e \), (2) increased \( R_c \), and (3) a very large and thin ischemic zone. In other circumstances it leads to ST elevation on the overlying epicardium.\(^{14-16,42}\) The finding that under some circumstances an ST depression is obtained in overlying leads may help to explain the results of early experimental studies, which found ST depression on the epicardium overlying a subendocardial ischemic or injured region.\(^{11,13}\) A nontransmural ischemic zone large enough to provoke ST depression on the epicardium overlying its center has never been demonstrated in animal models. However, it may relate to the clinical presentation of circumferential subendocardial ischemia, which is characterized by ST depression in overlying precordial leads.\(^{5,6}\)

The anisotropy in propagation velocity in cardiac tissue is promoted by both intracellular and extracellular anisotropic conductivity. In contrast, ST depression is favored by a decrease in \( R_e \) and by an increase in \( R_c \). Thus, both factors may contribute to ST depression while cancelling their contributions to anisotropic propagation. Therefore, measurement of propagation velocity alone does not suffice to study the conductivity changes in ischemic or hypertrophic myocardium.

Comparison with other simulation studies
Several investigators have simulated ischemia, both with isotropic and anisotropic models.\(^{14,16,17,43-46}\) Johnston et al\(^{45}\) have explicitly pointed out the importance of anisotropy in mathematical models of ischemia. MacLachlan et al\(^{17}\) have shown differences in transmural ST deviation patterns between isotropic and anisotropic myocardium for a heart embedded in a human torso. Early theoretical work using, by necessity, an isotropic myocardium, predicted ST elevation in transmural ischemia and ST depression in subendocardial ischemia.\(^{47}\) Li et al\(^{14}\) used an isotropic myocardium, but mimicked the effect of anisotropy by regional variation of the injury current. This study, as well as all later work using a more realistic anisotropic myocardium, predicted ST elevation even in subendocardial ischemia.\(^{16}\) Depression was found over the lateral borders of the partial-thickness ischemia, the same location as in full-thickness ischemia.

Apart from the tissue conductivity values, the intracav-odynamic blood influences ST deviation\(^{48}\) (Figure 2). Johnston et al\(^{45}\) predicted ST depression in a model study with a simplified anatomy using anisotropy ratios very close to ours, which may be due to the infinite blood mass used in their study. Recently, Hopenfeld et al\(^{48}\) have shown ST depression overlying a subendocardial ischemia with 10% transmural extent. We have extended this finding for 30%–40% transmural extent and have shown that for larger diameters ST depression can be obtained with a larger transmural extent (Figure 5). In addition, we have shown how size and extent interact with \( R_e \) (Figure 5).

We have used a realistic profile of resting \( V_m \), based on assumptions on the extrusion and diffusion of \( K^+ \).\(^{28}\) Regardless of the validity of these assumptions, the resulting profiles of \( [K^+]_o \) and \( V_m \) resemble measured profiles\(^{28,49}\) better than those used in earlier studies.\(^{14,16,17,45}\)

Limitations
We have shown that all four bidomain conductivities play a role in determining ST deviation. Unfortunately, these values are not accurately known.\(^{46}\) Measuring anisotropic bidomain conductivity is technically challenging and has only been done in papillary muscles.\(^{50-52}\) Conductivity changes in ischemia have been measured, but anisotropy was not reported.\(^{53}\) For a complete understanding of ST deviation, better estimates of these values are sorely needed.\(^{15}\)

It is tempting to extrapolate our results to the ECG. This would allow comparison with many clinical and experimental studies. However, the relation between heart and surface potentials is complex. An anisotropic model of the heart coupled to an inhomogeneous torso model is required to predict ST deviation in the ECG.

Conclusion
In healthy myocardium, both transmural and compact subendocardial ischemic zones lead to epicardial ST elevation. Ischemia is likely to occur in tissue that is subject to a remodeling of anisotropic conductivity. We have shown that a reduction of \( R_e \), an increase in \( R_c \), or a sufficiently large and thin ischemic zone can explain ST depression in epicardial leads. These findings may help to explain the equivocal results that have been obtained in experimental endocardial ischemia or injury and to better understand the cause and nature of ST segment changes in clinical settings.

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